

# Grosvenor Road Primary School

# **Calculations Policy**

Incl. Fractions Policy and KS2 Vocabulary List

**Updated September 2023** 

This policy outlines how calculations are to be taught at Grosvenor Road Primary School. Teachers should use it alongside the Mathematics policy to deliver a consistent approach towards calculations. The policy aims to assist teachers in delivering a programme geared towards mastery of Mathematics in line with The National Curriculum (DfE 2014)

#### Our Aim at Grosvenor Road

Each child should be able to think and solve problems mathematically by using the appropriate skills, concepts and knowledge. They should be provided with rich and enjoyable experiences related both to their individual needs and to the wider requirements of society.

We aim for each child to:

1. **Be Positive** - they develop a curious, inquisitive and positive approach to Mathematics as a subject- a 'can do attitude'.

2. **Be Fluent** – over time they have a conceptual understanding of mathematics and the can recall key facts easily.

3. **Solve Problems** – they can apply skills to unfamiliar problems, they can break a problem into key parts and they persevere to find a solution.

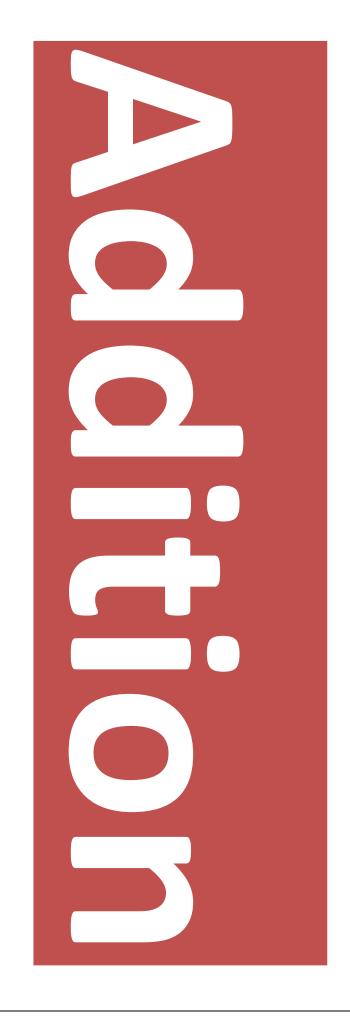
Taken from the school's mathematics policy

As a school, we aim to use this policy to develop children who are numerate thinkers and that have a concrete understanding of the fundamentals of Mathematics. Children are taught using shared language and a consistent approach towards resources, images and models. The following resources are used throughout the school in order to underpin a child's learning:









#### Early learning Goal:

### Have a deep understanding of number to 10, including the composition of each number: subitise up to 5; automatically recall number bonds to 5 and some number bonds to 10, including double facts.

Children should be encouraged to develop their own mental picture surrounding numbers in preparation for calculation. They should be given a wide range of opportunities to experiment with Addition in practical scenarios, e.g. role play, counting games and small world play. Children should be given access to a wide range of mathematical resources for counting so that they are aware of them and how they can be used later in the school. Children should begin to identify their own mathematical problems based on their own interest and fascinations using the resources and equipment made available to them.

#### **Counting all method**

Children will begin to develop their ability to add by using practical equipment to count out the correct amount for each number in the calculation and then combine them to find the total.

#### Counting on method

To support children in moving from a counting all strategy to one involving counting on, children should still have two groups of objects but one should be covered so that it cannot be counted, children should be encouraged to use their knowledge of the order of numbers to count on mentally without the visual stimulus of the second group.

In Nursery, children are introduced to a sense of number through Numicon. This should be further developed in Reception: using the **Firm Foundations Numicon kit**.



On top of this, children in Nursery also develop their number skills and confidence through 'Let's visit Numberland.' This scheme gives the children the opportunity to underpin their knowledge of number through practical activities, songs and free play, which helps to give a context for problem solving at an early age. This should continue to be developed in reception using the '**Let's visit** 

Numberland' handbook.

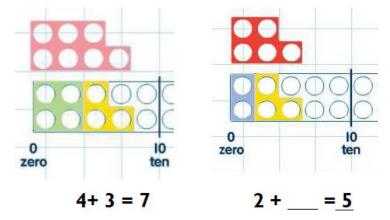






Add 1 and 2 digit numbers up to 20 using concrete objects and pictorial representations.

Children should continue to use a wide range of mathematical apparatus and jottings to approach Addition. They should combine separate groups of objects to find a total using the counting all or counting on method initially approached in EY. Children should also continue to use **Numicon Kit 1** to underpin mental methods and their understanding of number. For further in depth guidance on the use of Numicon, please consult the **Numicon Handbook**.



Alongside Numicon, the children should also be introduced to Base 10 equipment in preparation for the move to formal Addition and place value.

The children can make numbers using the Base 10 equipment using a mixture of 'ten rods' and 'ones cubes' to create numbers greater than 10 but less than 20.



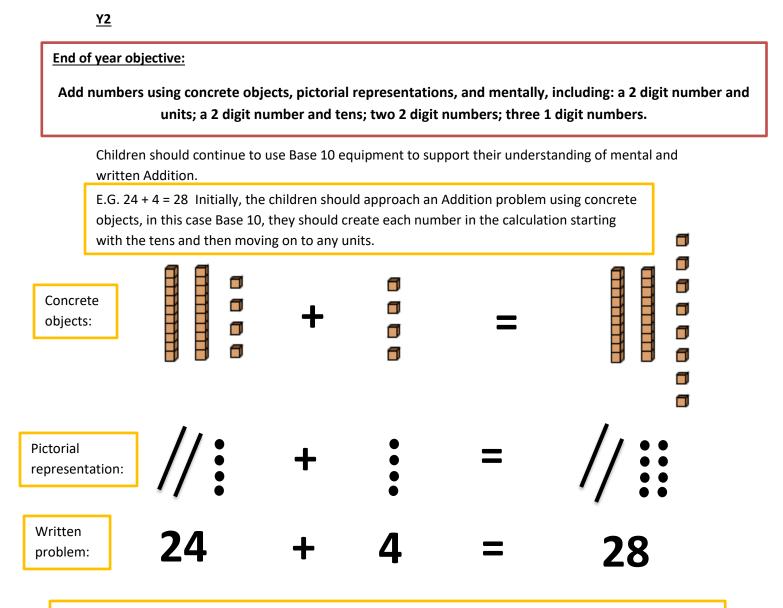
Here we can see the number 12 made up of a ten rod and 2 one cubes. This can then be added to as the support for the calculation of an Addition problem.

Above, the child has added further one cubes to the initial number of twelve to create 18. In this case the child could group the one cubes together to aid with counting. Where possible the child should be encouraged to record this problem as 12 + 6 = 18 using the correct mathematical symbols.

#### Children should also be able to:

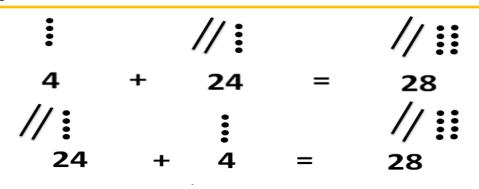
- Read, write and understand Addition problems using the Addition (+) and Equals (=) symbols.

- Solve one step Addition problems including missing number problems.
- Represent and use number bonds to 20.

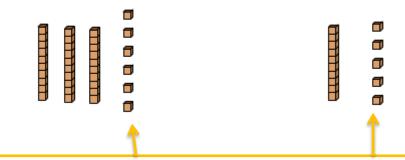


When drawing a pictorial representation of the calculation using Base 10 apparatus, the children should be taught and encouraged to represent a 10 rod using a slanted line and dots for the ones blocks. Underneath each pictorial representation the children should be encouraged to write the value of each diagram to familiarise themselves with written calculations.

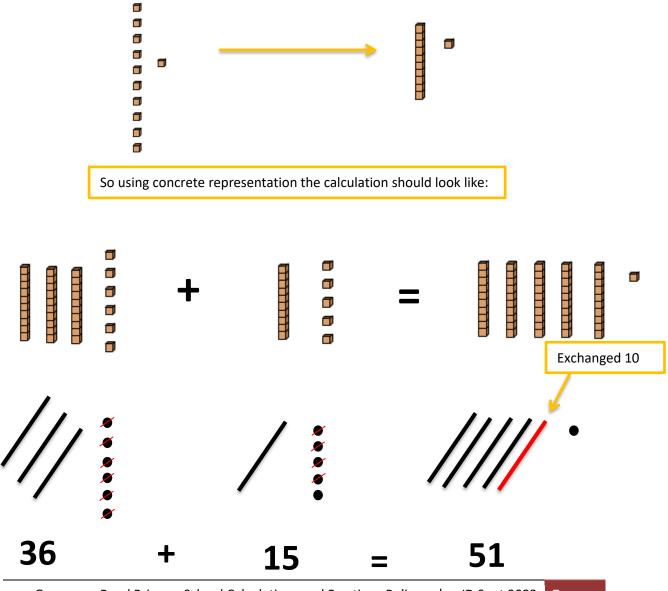
The children should be taught to recognise that Addition is **commutative** and that the numbers can be rearranged within the calculation.



The children should continue to use this method when exchanging is required. When the units total more than 10, the children should be taught and encouraged to exchange 10 ones cubes for a 10 rod in preparation for exchanging within Formal Columnar Addition. For example, in the calculation 36 + 15 = 51, the children would start by creating each number using the Base 10 apparatus.

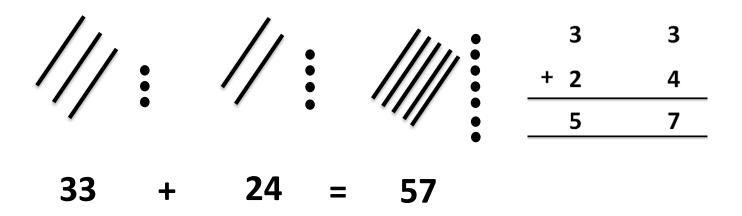


6 ones blocks + 5 ones blocks = 11 ones blocks. Within this calculation the children should recognise that 11 one blocks can be exchanged for one 10 rod and a single one block



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As the children become more confident with Addition they should begin to layout the written calculation using the formal method alongside the pictorial representation in preparation for the move to Formal Columnar Addition in Y3.

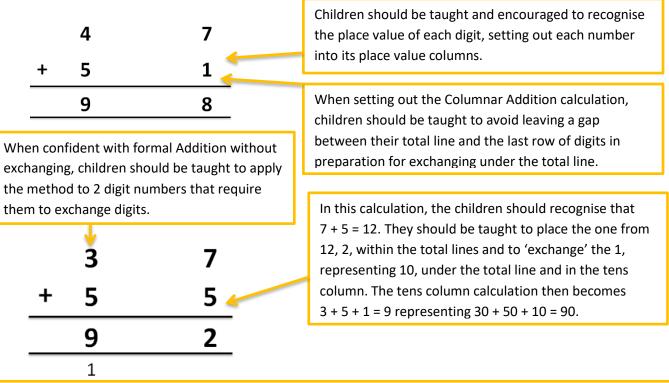


The children should be taught and encouraged to set the digits out into their place value columns writing the total of the calculation in between the two total lines.

- Use concrete and pictorial resources to solve Addition problems in context and missing number problems.
- Use inverse operations to solve problems and check the accuracy of an answer.
- Recall and use Addition and Subtraction facts to 20 fluently, and derive and use related facts up to 100.

#### Add numbers using formal written methods (Columnar) with numbers up to and including 3 digits.

Children should build upon their knowledge of Addition from Y2 and move towards formal written Columnar Addition with numbers up to and including 3 digits. Initially, children should work on numbers that do not require exchanging to cement the skill and to re-familiarise themselves with the layout.



Once the children have become confident with the layout and conventions of Columnar Addition with 2 digit numbers and exchanging, they should introduce the skill to 3 digit numbers. Children should be taught and encouraged to recognise that it is not always a 'ten' that is exchanged.

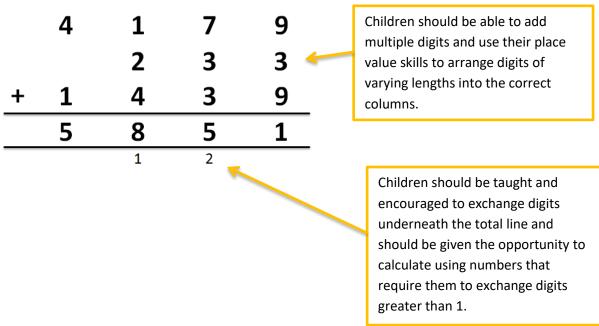
↓ 4	8	7
+ 2	3	2
7	1	9
1 🔶		

In this calculation, the children should recognise that 8 + 3 = 11 represents 80 + 30 = 110. As the 0 has no value it does not need to be added to the total. The 1, representing 10, should be written into the tens column of the total line and the 1, representing 100, should be exchanged under the total line in the hundreds column before being added to the total for this column.

- Add numbers mentally including: a three digit number and a 1 digit number; a 3 digit number and a 2 digit number and a 3 digit number and a 3 digit number.
- Estimate and use inverse operations to check the accuracy of an answer.
- Solve a range of Addition problems including missing number problems.

Use formal written methods (Columnar) to add multiple whole numbers with up to 4 digits.

Children should continue to use and build on formal Addition skills that have been learnt in Y3 and apply these skills to increasingly larger numbers and calculations that involve multiple numbers of varying sizes.



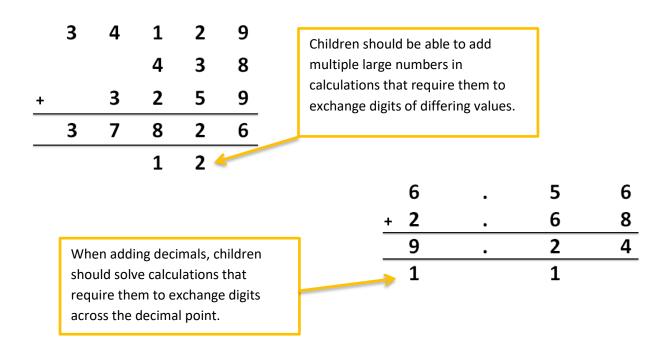
- Use estimation, inverse operations and rounding to check the accuracy of an answer, both in and out of context.
- Solve two step Addition and Subtraction problems in context, deciding which operation to use and when.
- Solve simple measure and money problems involving fractions and decimals to 2 decimal places.

Liam, Sarah and Amy buy lunch at a salad bar.						
		salad bar				
	Salads Desserts					
	cheese	£1.20	banana	25p		
	egg	90p	apple pie	50p		
	tuna	£1.60	yogurt	35p		
Liam has £2.50 to	Liam has £2.50 to spend.					
He buys a tuna salad and an apple pie.						
How much money has he got left?						

Circle <b>three</b> nu	umbers that a	add to make 7	50.	
🌯 450	350	250	150	50

Use formal written methods (columnar) to add multiple digits ranging in size from 2 d.p. to 5 digit whole numbers.

Building on what has been taught in Y4, children will continue to use and apply their knowledge of Columnar Addition to increasingly larger numbers and decimals.



#### Children should also be able to:

- Use rounding and estimation to check the accuracy of an answer within the context of a problem.
- Solve multi-step problems in context, choosing which operation to use and when.

"Pupils should go beyond the measurement and money models of decimals, for example, by solving puzzles involving decimals."

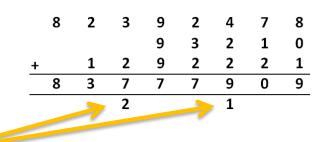
DfE - The 2014 Primary National Curriculum – Notes and Guidance

Pupils should be given the opportunity to use their problem solving and Addition skills in regards to decimals when looking at 'pure' problem solving situations outside of context.



To confidently use a formal written methods (Columnar addition) to add multiple decimals and whole numbers.

As part of the National Curriculum, children should be confident with Columnar Addition using digits of varying sizes, from 8 digit whole numbers to decimals with 3 decimal places.



Children should be able to add multiple large numbers requiring them to 'exchange' digits of varying values.

2	3	3	6	1
	9	0	8	0
5	9	7		0
+	1	3	0	0 ←
9	3	5	1	1
2	1	2		

Children should continue to use their knowledge of place value to set out numbers of varying sizes, when doing this, children should be taught and encouraged to write the numbers in the same number of decimal places through identification. For example, 3 tenths is the same as 300 thousandths and thus 0.3 is the same value as 0.300.

#### Children should also be able to:

- Apply written Addition skills when solving multi-step problems in context.

E.G.	Т	These are some prices in a fish and chip shop.					
		Fish £2.30 Peas 35p					
	Sausage £1.80		Curry sauce 40p				
		Chips (small bag) 60p	Bread roll 30p				
		Chips (large bag) 90p	Pickled onion 28p				

Megan buys a sausage and a bread roll. Chen buys a small bag of chips and a curry sauce. How much **more** does Megan pay than Chen?

- Identify missing digits within Columnar Addition problems.

E.G.	3 4 7	3 4 7 6
	1 7 5	1 5 7 5
	5 0 5 1	5 0 5 1

#### Early learning Goal:

### Have a deep understanding of number to 10, including the composition of each number: automatically recall number bonds to 5, including subtraction facts.

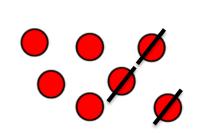
Children should be encouraged to develop their own mental picture surrounding numbers in preparation for calculation. They should be given a wide range of opportunities to experiment with Subtraction in practical scenarios, e.g. role play, counting games and small world play. Children should be given access to a wide range of mathematical resources for counting so that they are aware of them and how they can be used later in the school. Children should begin to identify their own mathematical problems based on their own interest and fascinations using the resources and equipment made available to them.

#### <u>Taking away</u>

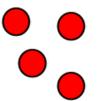
E.G.

Children should begin to develop their own mental understanding of Subtraction and should be supported with apparatus when doing so. They should begin to use a wide range of mathematical apparatus and resources to subtract two single digit numbers.

7 - 3 = 4



Children should start by counting out the initial number of counters before removing or covering the second number of counters. They should then solve the calculation by counting the remaining number of counters.



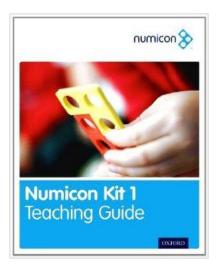
As the children become more confident with number and counting they should be encouraged to count back to find their answer. In this case starting at 7 and counting back 3 numbers, arriving at the answer of 4.

Further information and guidance for the teaching of Subtraction should be taken from the **Numicon Firm Foundations Teaching Guide.** 



#### Subtract 1 and 2 digit numbers up to 20 using concrete objects and pictorial representations.

Children should continue to use practical apparatus and mathematical resources when approaching Subtraction. They should build upon taking away skills learnt in Reception and begin to record calculations using a range of jottings as well as using the appropriate mathematical symbols in more formal recordings. Children should also continue to use **Numicon Kit 1** to underpin mental methods and their understanding of number. For further in depth guidance on the use of Numicon, please consult the **Numicon Handbook**.



Alongside Numicon, the children should continue to use Base 10 equipment in preparation for a move to formal calculations. Initially, the children should focus on using groupings of one cubes for Subtraction to avoid having to exchange. As confidence and accuracy with Subtraction grows, the children may begin to approach exchanging ten rods for one cubes with calculations.

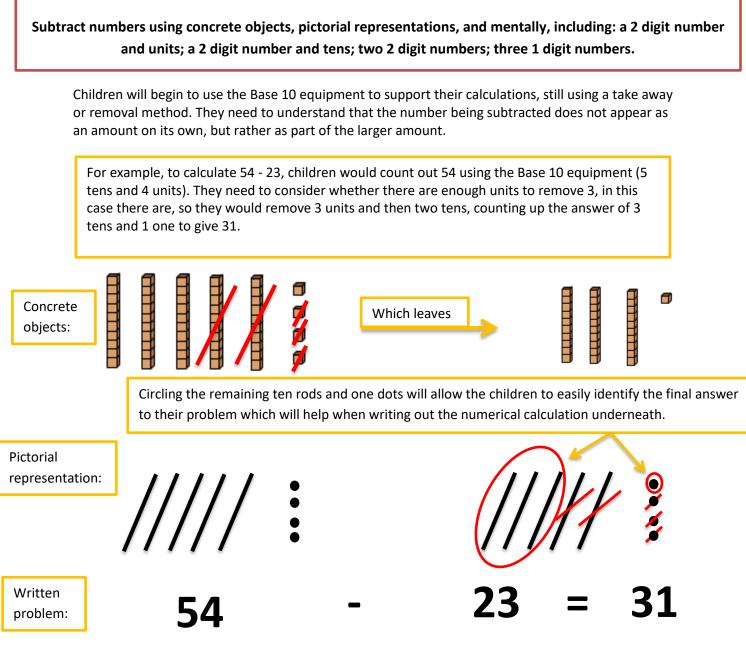


12 – 4

Where possible, the children should be taught and encouraged to record the calculation using the appropriate mathematical symbols for the calculation.

Above we can see the child has counted out the initial number of 12 before removing the 4 counters as is stated in the written calculation. The children should be taught and encouraged to 'count away' the counters they are removing and then count the remaining counters in order to increase accuracy.

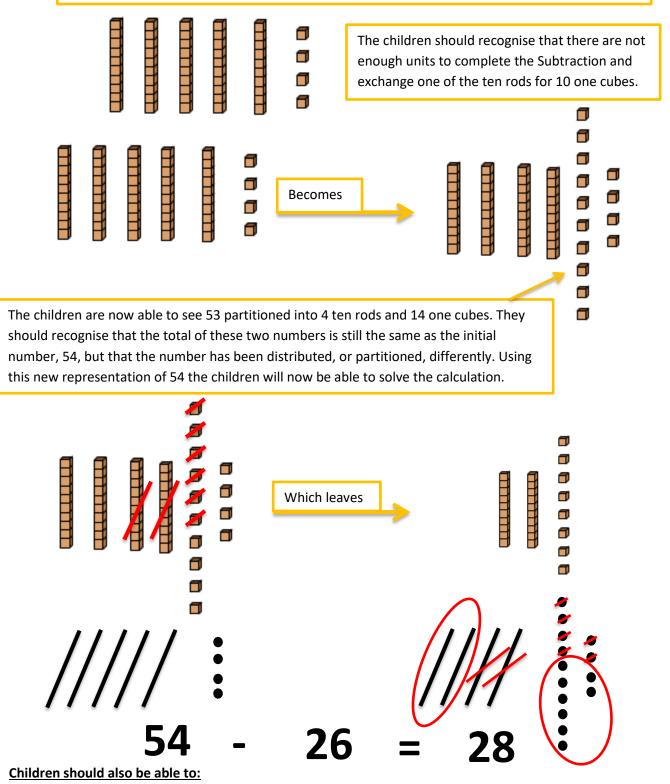
- Read, write and understand Subtraction problems using the Subtraction (-) and Equals (=) symbols.
- Solve one step Subtraction problems including missing number problems.
- Represent and use Subtraction facts to 20.



Children should be taught and encouraged to include the written problem underneath their pictorial representation to further reinforce the value of each diagram. This will also help with the transition into written calculations.

End of year objective:

When the number of units to be subtracted is greater than the number of units in the initial number the children must be taught and encouraged to recognise that they need to exchange a ten rod for 10 one cubes in order for the calculation to be completed successfully. For example, 54 - 26 = 28. As with all Subtractions the children would start by counting out 54 using the Base 10 apparatus.



- Use concrete and pictorial resources to solve Subtraction problems in context and missing number problems.
- Use inverse operations to solve problems and check the accuracy of an answer.
- Recall and use Addition and Subtraction facts to 20 fluently, and derive and use related facts up to 100.

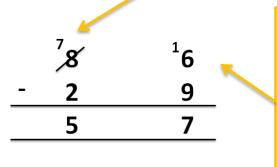
Subtract numbers using formal written methods (Columnar) with numbers up to and including 3 digits.

Children should continue to build upon mental methods for Subtraction learnt in Y2 throughout Y3, alongside this the children should be taught and encouraged to use Formal Written Subtraction, Columnar, as a means for calculating with larger numbers.

	8	7	4
-	5	2	3
	3	5	1

Initially, children should be introduced to formal Subtraction with a range of numbers that does not require exchange to calculate. They should be expected to set out their digits into the appropriate place value columns and recognise the value that each digit represents.

Once the children are confident with the layout of Formal Written Subtraction they should be taught to calculate with digits that require an exchange. The children should be taught and encouraged to strike through the number from the next place value column in order to solve the calculation.



In this calculation we can see that the initial stage should be 6 - 9. Within Column Subtraction we are unable to include negative numbers as part of our answer so we need to exchange a ten from the next column for 10 units. The calculation then becomes 16 - 9 = 7. As we have exchanged 10 units from the 8, representing 80, in the tens column this number is now 10 units lower and thus the 8 becomes 7 in the calculation.

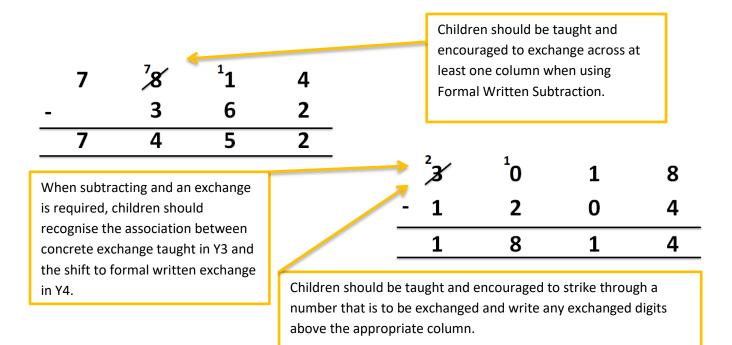
As the children become more fluent with the calculation and its layout, they should begin to calculate using increasingly larger numbers and numbers of differing digit lengths using their place value skills to set the digits out into the correct columns to avoid miscalculation.

<sup>8</sup> ⁄9	<sup>1</sup> <b>3</b>	6
-	4	1
8	9	5

- Subtract numbers mentally including: a 3 digit number and a 1 digit number; a 3 digit number and a 2 digit number and a 3 digit number.
- Estimate and use inverse operations to check the accuracy of an answer.
- Solve a range of Subtraction problems including missing number problems.

#### Use formal written methods (Columnar) to subtract numbers with up to 4 digits.

Children should continue to use and build on formal Subtraction skills learnt in Y3 and apply these to numbers with up to 4 digits. Children should also be able to subtract numbers of differing digits.



- Use estimation, inverse operations and rounding to check the accuracy of an answer, both in and out of context.
- Solve two step Addition and Subtraction problems in context, deciding which operation to use and when.
- Solve simple measure and money problems involving fractions and decimals to 2 decimal places.

Emily has these coins.	Write the two missing digits.
	1 - 2 = 34
How much more money does Emily need to make exactly £5?	Write two numbers, each greater than 100, to complete this subtraction. $ \begin{array}{c} & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & $

To subtract numbers with more than 4 digits, including numbers to 2 d.p., using formal written methods (Columnar).

Building on what has been taught in Y4, children should continue to use and apply their use of Columnar Subtraction to increasingly larger numbers and decimals.

increas	subtracting nu singly larger si expected to e			<sup>4</sup> 5	<sup>1</sup> <b>4</b>	<sup>7</sup> <b>8</b> ′	<sup>1</sup> <b>3</b>	8
multip	le columns.			—	5	7	6	4
			J	4	9	0	7	4
5		1						
_6		໋5	6		Children sl			
3		6	1		numbers c align the d	-	-	
2	•	9	5		value colu	mns.		
2	•	9	5					

#### Children should also be able to:

- Solve multistep Subtraction problems in context and decide what operation to use when.
- Use rounding and estimation to check the accuracy of an answer.

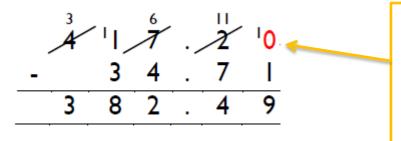
"Pupils should go beyond the measurement and money models of decimals, for example, by solving puzzles involving decimals."

DfE - The 2014 Primary National Curriculum – Notes and Guidance

Children should again be given the opportunity to use problem solving skills involving the Subtraction of decimals outside of a context as stated within the Addition guidance.

To subtract a range of whole and decimal numbers confidently using formal written methods (Columnar Subtraction).

Children should build on their use of decomposition and apply this to use with digits ranging from numbers with three decimal places to 8 digit whole numbers.



When subtracting numbers of differing decimal places, children should be taught that they are the same through identification and that 2 tenths is the same as 20 hundredths, therefore 0.2 is the same value as 0.20.

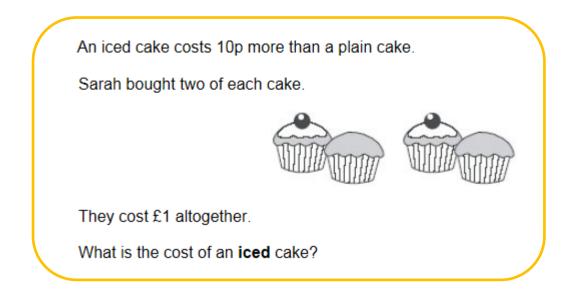
When subtracting increasingly larger numbers children will be expected to exchange across multiple columns.

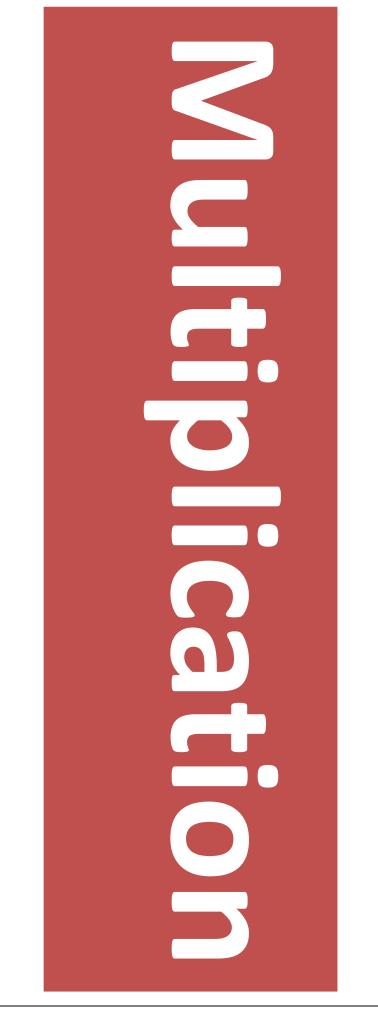
	4	<sup>1</sup> ¥	<sup>16</sup>	<sup>18</sup> 9	<sup>1</sup> 8	5	⁵ <b>6</b> ∕	<sup>1</sup> 8	
-	1	0	8	9	9	2	3	9	
	3	1	8	9	9	3	2	9	

#### Children should also be able to:

- Solve multistep Subtraction problems in context and when combined with other operations.

E.G.





#### Early learning Goal:

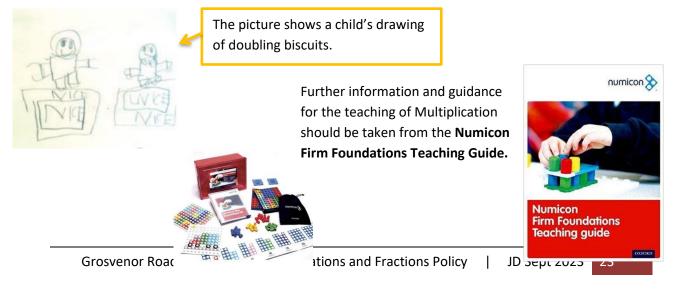
Explore and represent patterns with numbers up to 10, including double facts.

Children should be encouraged to develop their own mental picture surrounding numbers in preparation for calculation. They should be given a wide range of opportunities to experiment with Multiplication and grouping in practical scenarios, eg role play, counting games and small world play. Children should be given access to a wide range of mathematical resources for counting so that they are aware of them and how they can be used later in the school. Children should begin to identify their own mathematical problems based on their own interest and fascinations using the resources and equipment made available to them.

Children should also be given the opportunity to experiment with various 'real world' objects that show Multiplication and grouping through the use of non-formal groupings and arrays.

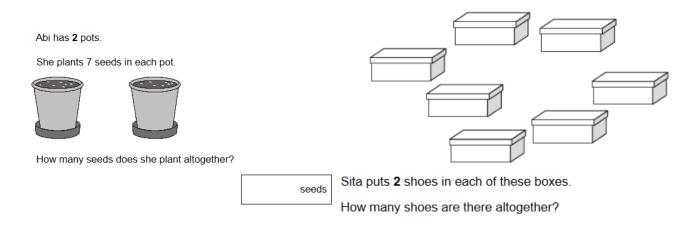


Children should also be encouraged to develop their own ways of recording 'real world' Multiplication through drawings and jottings.

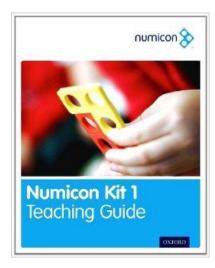


Solve one-step problems involving Multiplication, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher.

Children should continue to use a wide range of practical equipment as a mean of solving Multiplication problems with the support of the teacher. They should use a wide variety of 'real world' objects that show Multiplication as an array, such as egg boxes, ice cube trays, cake tins and chocolate bars. In Year One, children should begin to approach one step problems using concrete resources and pictorial representations to underpin their learning.



Children should also continue to use Base 10 and Numicon equipment. Further in depth guidance can be found in the Numicon Kit 1 Handbook.

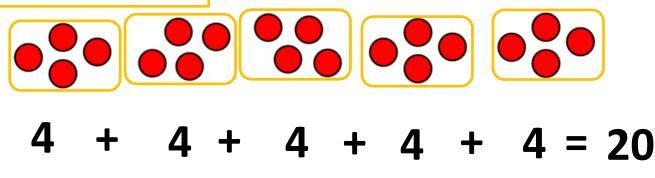




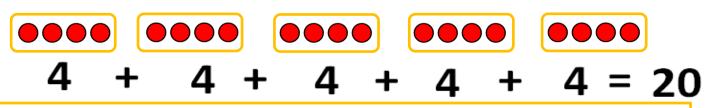
Calculate mathematical statements for Multiplication *(using repeated Addition)* and write them using the Multiplication (x) and Equals (=) signs.

Children should be taught to calculate Multiplication through repeated Addition supported by the use of practical apparatus, e.g. Base 10, Numicon, counters or cubes etc. Children should initially approach Multiplication at this stage through the 2, 5 and 10 Multiplication Tables.

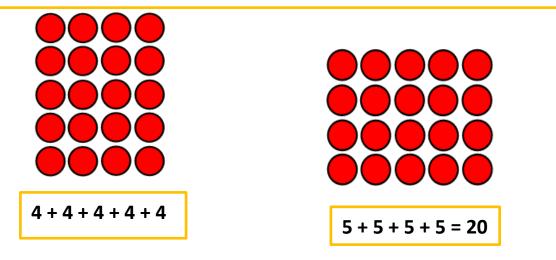
5 x 4 = 20 can be shown using 5 equal groups of 4 counters. Initially the children should begin to group the counters together in to random groupings as below.



As children become more confident with Multiplication they should be encouraged to arrange the counters, or other apparatus in a more organised pattern, as shown below. This will help with the transition into use of arrays.



Children should continue to use and adapt this method of Multiplication into the use of arrays, this helps to reinforce the commutative nature of Multiplication and will help with the transition into Formal Multiplication.



Throughout Y2 children should be encouraged to use a range of apparatus and jottings when multiplying numbers in order to improve understanding and fluency with calculations.

# 5 x 4 = 20

## 4 x 5 = 20

Children should be taught and encouraged to use mathematical symbols when writing out the numerical problem of each Multiplication calculation.

Children should also be taught and encouraged to recognise that Multiplication is commutative, and thus the Multiplier and the Multiplicand are interchangeable.

- Solve problems involving Multiplication and Division, using materials, arrays, repeated Addition, mental methods, and Multiplication and Division facts, including problems in contexts.
- Recall and use Multiplication and Division facts for the **2**, **5** and **10** Multiplication Tables, including recognising odd and even numbers

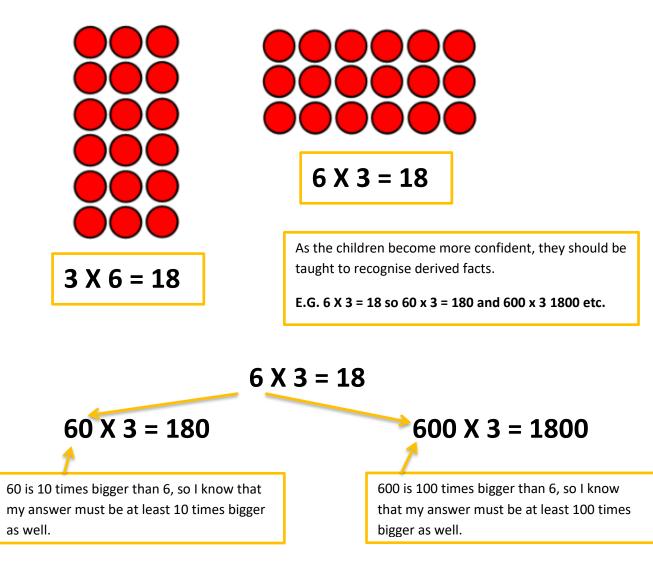
#### To practise and recall mental methods for Multiplication, progressing towards formal written methods for Multiplication (Short Multiplication).

Children should continue to work towards a formal method for Multiplication throughout Y3. They should build upon knowledge of repeated Addition and Multiplication Tables facts from Y2 and continue to use concrete objects and apparatus to underpin their learning.

#### Stage 1

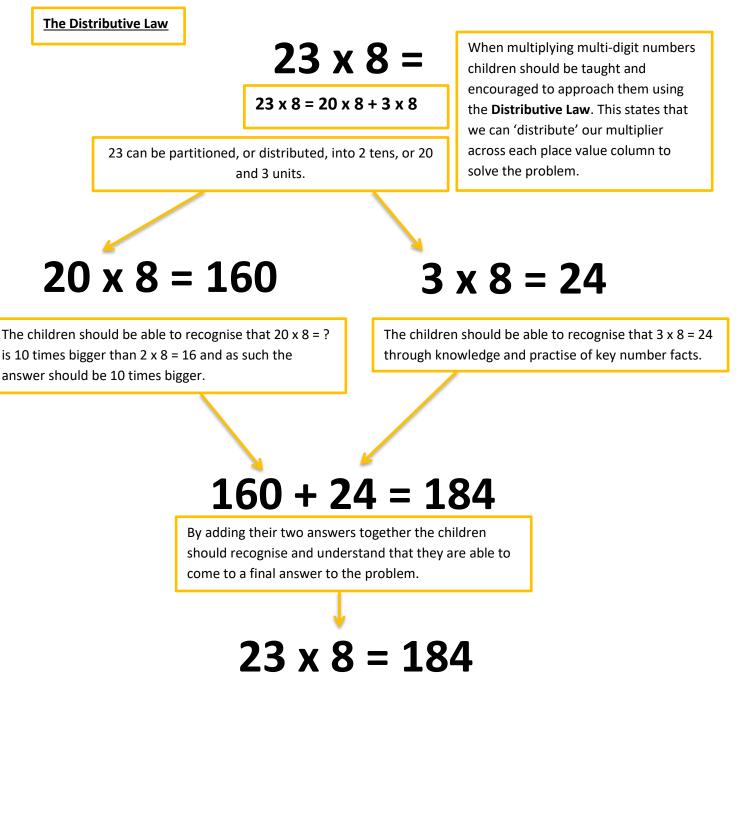
Children should be introduced to the 3, 4 and 8 Multiplication Tables and learn through use of concrete objects and arrays that these can be displayed and written in many different ways. Children should be taught and encouraged to recognise that Multiplication facts are **Commutative**.

E.G.



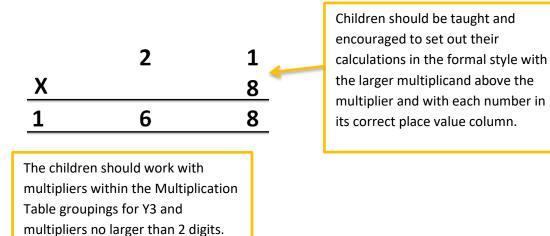
#### Stage 2

Children should use partitioning and the **Distributive Law** when multiplying larger numbers to help them segment the digits into number facts that can be derived from times table knowledge. This will help the children to make the step towards Formal Short Multiplication and to underpin the children's understanding between number facts and the answers given in the different stages of Formal Multiplication.

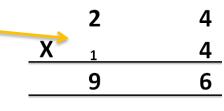


#### Stage 3

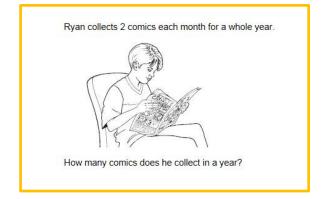
As the children become confident in both key number facts and the Distributive Law, they should move towards Formal Short Multiplication with 2 digit numbers.

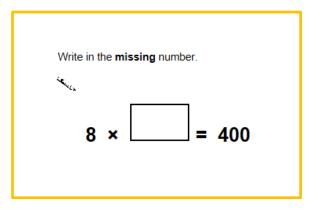


When needed, children should exchange any digits above the next digit in the corresponding place value column. For example, 4 X 4 = 16 so the 6 units will be placed within the total lines and the 1, representing 10, should be placed above the total line in the tens



- Recall and use Multiplication and Division facts for the **3**, **4** and **8** Multiplication Tables.
- Solve problems, including missing number problems, involving Multiplication and Division relating to known facts.





Multiply 2 and 3 digit numbers by a 1 digit number using formal written layout (Short Multiplication).

Children should recap on the formal written methods taught at the end of Y3 and expand upon these during their time in Y4.

	2	4
x	2	6
1	4	4

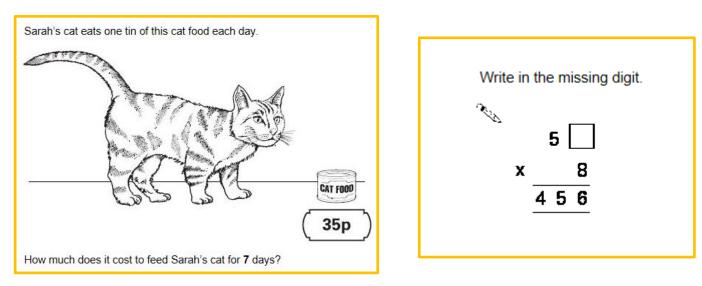
to exchange multiplied digits above the digit in the next column. Children should be expected to move towards exchanging across multiple columns within Formal Short Multiplication.

Children should be taught and encouraged

Children should move towards multiplying 3 digit numbers by 1 digit numbers.

	3	4	2
х	2	1	7
2	3	9	4

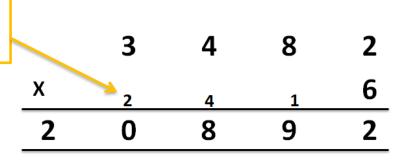
- Recall Multiplication and Division facts up to 12 x 12 (Statutory Requirement)
   As part of the national curriculum, children are required to be confident in their knowledge of all key Multiplication Tables by the end of Y4.
- Solve Multiplication and Division problems in context.



### Multiply numbers up to 4 digits by a 1 or 2 digit number using a formal written method, including Long Multiplication for 2 digit numbers.

Children should extend their knowledge of Short Multiplication learnt in Y4 to Formal Long Multiplication. Children should move towards multiplying 3 and 4 digit numbers by a 2 digit multiplier.

Children should be taught and encouraged to exchange multiplied digits above the number in the next columns when needed.



When calculating using Formal Short Multiplication, children should be taught to exchange across multiple columns.

	3	5	1	3
х	2		1	4
1	2 <b>4</b>	0	5	2
3	5	1	3	0
4	9	1	8	2

When calculating using Formal Long Multiplication children should be taught and encouraged to exchange multiplied digits above the number in the next column. When applicable, during the final addition stage of the calculation children should write any exchanged digits beneath the total line to help avoid miscalculation when totalling an answer.

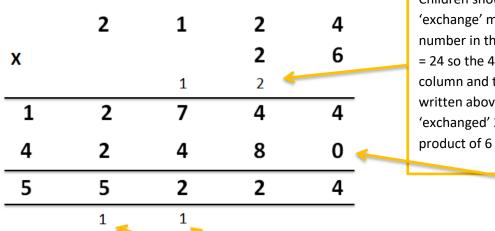
#### Children should also be able to:

- Identify Multiples and Factors, including finding all factor pairs of a number, and common factors of 2 numbers.
- Multiply and divide whole numbers and those involving decimals by 10, 100 and 1,000.
- Solve problems involving Multiplication and Division, including using their knowledge of
- Y6 Factors and Multiples, Squares and Cubes

#### End of year objectives:

- Multiply multi-digit numbers, up to 4 digits by 2 digit whole numbers, using the formal written method of Long Multiplication.
- Multiply 1 digit numbers with up to 2d.p. by whole numbers using formal written methods where the answer has up to 2d.p.

Children should build upon the skills learned in Y5 to become confident in the multiplication of larger numbers.



Children should be taught and encouraged to 'exchange' multiplied digits above the number in the next column. For example 6 x 4 = 24 so the 4 would be written into the units column and the 2, representing 20, would be written above the next column. The 'exchanged' 2 would then be added to the product of 6 and 2.

When finding the final answer to the calculation, the children should be taught and encouraged to write any 'exchanged' digits from their addition underneath the total line. This will help to avoid miscalculation when totalling an answer. When multiplying by two digit numbers, children should be taught and encouraged to recognise that the second stage of the calculation takes place with numbers that are ten times larger and thus '0' should be introduced as a place holder.

When multiplying decimals by whole numbers children should be taught and encouraged to write each number to the same number of decimal places through identification. For example, 4 units have the same value as 400 hundredths.



Children should be taught to recognise that whenever a number is multiplied by 0 the answer will always be 0 and as such, they can increase the efficiency of their calculation by viewing these digits as place holders within the layout of the formal method.

- Identify Common Factors, Common Multiples and Prime Numbers
- Use estimation to check that an answer is correct within the context of a problem.
- Solve multi-step problems in context that incorporate Multiplication as at least one of the steps.

7 

#### Early learning Goal:

Explore and represent patterns with numbers up to 10, including how quantities can be distributed equally.

Children should be encouraged to develop their own mental picture surrounding numbers in preparation for calculation. They should be given a wide range of opportunities to experiment with Division and sharing in practical scenarios, e.g. role play, counting games and small world play. Children should be given access to a wide range of mathematical resources for counting so that they are aware of them and how they can be used later in the school. Children should begin to identify their own mathematical problems based on their own interest and fascinations using the resources and equipment made available to them.

Children should also be given the opportunity to experiment with various 'real world' objects that show Division and sharing through the use of non-formal groupings and arrays.



Children should also be encouraged to develop their own ways of recording 'real world' Division through drawings and jottings.



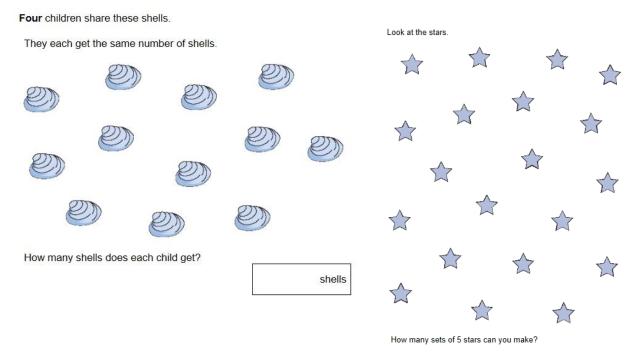
The picture shows a child's drawing to solve the problem, 'Can 8 be shared equally between 2?' The child has contextualised the problem through birds and eggs, sharing and linking 4 eggs to each bird.



Further information and guidance for the teaching of Division should be taken from the **Numicon Firm Foundations Teaching Guide.** 

## Solve one-step problems involving Division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher.

Children should continue to use a wide range of practical equipment as a mean of solving Division problems with the support of the teacher. They should use a wide variety of 'real world' objects that show Division as an array, such as egg boxes, ice cube trays, cake tins and chocolate bars. In Year One, children should begin to approach one step problems using concrete resources and pictorial representations to underpin their learning. Children should begin to recognise Division as the opposite of Multiplication as a means for solving problems.



Children should continue to approach Division problems, such as the one above, through 'grouping' or 'sharing'. They should be introduced to remainders and begin to describe them as 'left over' and identify that Division does not always leave you with fully equal groups.

Children should also continue to use Base 10 and Numicon equipment. Further in depth guidance can be found in the Numicon Kit 1 Handbook.





Calculate mathematical statements for Division *within the Multiplication Tables* and write them using the Division (÷) and Equals (=) signs.

Children should be taught and encouraged to use a range of practical equipment and jottings to approach Division as grouping or repeated Subtraction.

## **30 ÷ 5 = 6**

Children should be taught and encouraged to recognise that the question above is asking them 'how many equal groups of 5 are in 30?' Division problems can be approached using similar apparatus to Multiplication as they are inverse.

This problem could be approached with counters, the children counting out 30 counters before dividing them into equal groups of 5 until no more counters remain as is shown below. The children should be encouraged to arrange them in an organised pattern to aid calculation accuracy.



Children should also be taught and encouraged to divide numbers that leave a remainder in this way:

# 21 ÷ 5 = 4 remainder 1

- Solve problems involving Multiplication and Division, using materials, arrays, repeated Addition, mental methods, and Multiplication and Division facts, including problems in contexts.
- Recall and use Multiplication and Division facts for the **2**, **5** and **10** Multiplication Tables, including recognising odd and even numbers

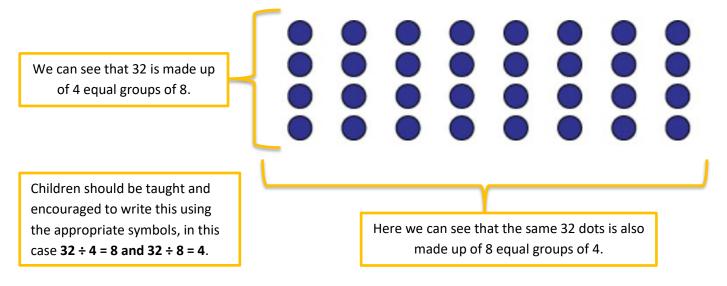
To practise and recall mental methods for Division, progressing towards formal written methods for Division.

#### Stage 1

Children should continue to build upon knowledge of grouping from Y2 and begin to apply this to increasingly larger numbers both in and out of context. From this point children should be introduced to inverse operations as a means of deriving number facts.

4 X 8 = 32 and so 32 ÷ 4 = 8 and 32 ÷ 8 = 4

This problem can be explained using an array:



#### Stage 2

Over the course of Y3, children should rehearse mental methods for Division, starting within Multiplication Tables facts and applying this skill to larger related numbers **e.g. 800**  $\div$  **4** = **200** can be derived from 80  $\div$  **4** = **20** and 8  $\div$  **4** = **2**.

In order to solve this problem the children should be taught and encouraged to use place value skills to recognise the relationship between 800 and 8 and what effect this has upon the answer.

# 80 ÷ 4 = 20

80 is 10 times bigger than my route calculation number so I know my answer will be at least 10 times bigger because of this.

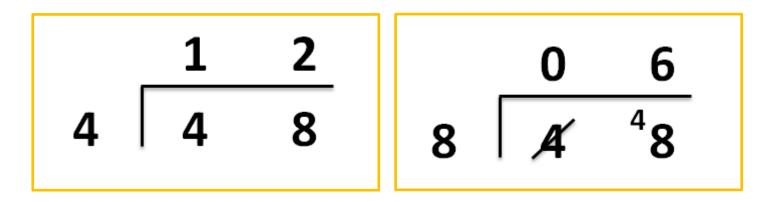
# 8 ÷ 4 = 2

800 ÷ 4 = 200

800 is 100 times bigger than my route calculation number so I know my answer will be at least 100 times bigger because of this.

#### Stage 3

Children should continue to practise derived Division facts from known Multiplication Tables. Alongside this children should be introduced to the Formal Short Division layout for Multiplication Tables facts. Within Formal Short Division Y3 children will not be expected to have final remainders.



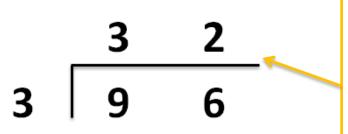
### Children should also be able to:

- Recall and use Multiplication and Division facts for the **3**, **4** and **8** Multiplication Tables.
- Solve problems, including missing number problems, involving Multiplication and Division relating to known facts.

#### End of year objective:

#### To use formal written methods (Short Division) to divide numbers without remainders.

Over the course of Y4 children should rehearse mental methods for Division, starting within Multiplication Tables facts and applying this skill to larger related numbers, **e.g. 600**  $\div$  **3 = 200 can be derived from 60**  $\div$  **3 = 20.** Children should then be taught and encouraged to use Formal Short Division to approach this problem by the end of Y4.



When the children are confident at setting out their work in this way, they should begin to use Formal Short Division with larger numbers, no greater than 3 digit whole numbers. All answers at this stage should be whole numbers and children should become confident at this stage before remainders are introduced.

For example, there is 1 group of 3 in 4 with 1 remainder. The answer, 1, is written above the total line and the remainder of 1 is then exchanged over to the next column and we see how many groups of 3 are in 12 before writing the answer above.

Children should also be able to:

- Recall Multiplication and Division facts up to 12 x 12
- Children should practise mental methods for Division facts, e.g.  $600 \div 3 = 200$  can be derived from  $60 \div 3 = 20$
- Solve Multiplication and Division problems in context.

Moving on from derived facts, children should be introduced to Formal Short Division, with 2 digit numbers. They should be taught and encouraged to write the number of groups above the total

line.

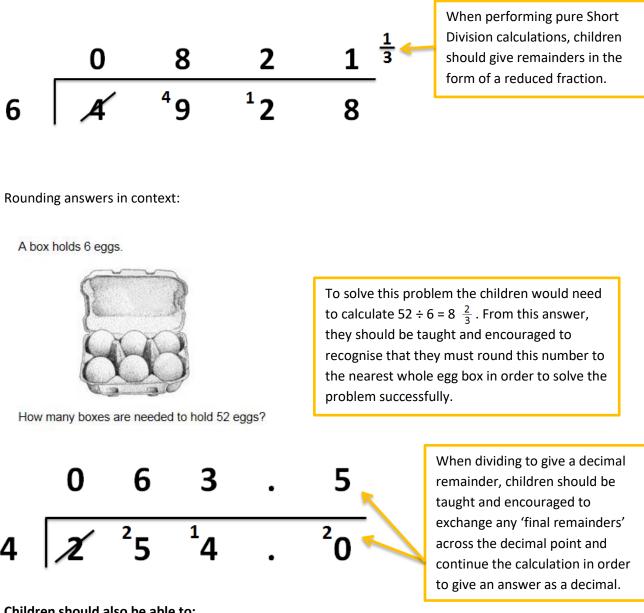
3 2 1 3 9 6 3

By the end of Y4, the children should be able to use Formal Short Division with 3 digit numbers to produce whole number answers. Within the calculation the children should be taught to exchange any remaining numbers over to the next column and include this within their calculation.

#### End of year objective:

Divide numbers up to 4 digits by a 1 digit number using the formal written method of Short Division and interpret remainders appropriately for the context.

Children should be taught to give remainders to Short Division calculations in a variety of formats, including fractions, rounded numbers and decimals. This should then be applied to a problem solving context where appropriate.



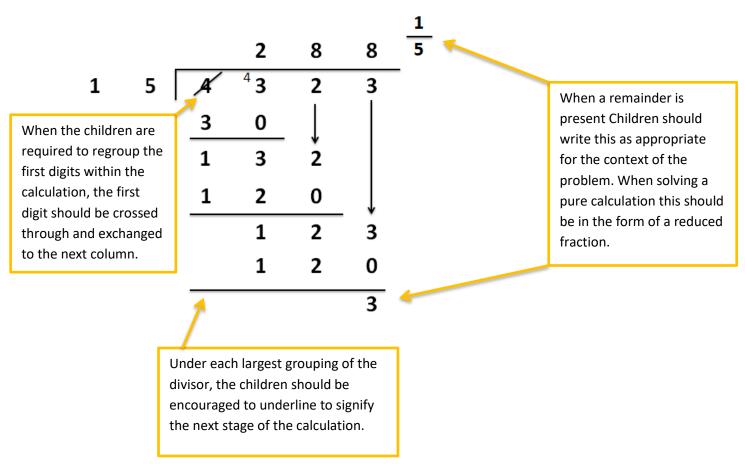
#### Children should also be able to:

- Multiply and Divide whole numbers and those involving decimals by 10, 100 and 1,000.
- Solve problems involving Multiplication and Division, including using their knowledge of Factors and Multiples, Squares and Cubes.

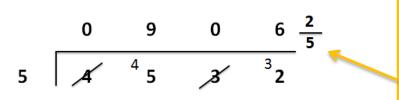
End of year objectives:

- Divide numbers of up to 4 digits by a 2 digit whole number using the formal written method of Long Division and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context.
- Divide numbers by up to 4 digits by a 1 digit number using the formal written method of Short Division where appropriate, interpreting remainders according to the context.

Children should build upon the knowledge of Short Division gained within Y5 and apply this skill to Formal Long Division with increasingly larger numbers.



The children should also be able to use and apply Formal Short Division when calculating with smaller numbers.



Within both elements of formal Division children should be taught and encouraged to use estimation and inverse operations to check the accuracy of their answer according to the context. As with Long Division, when a remainder is present Children should write this as appropriate for the context of the problem. When solving a pure calculation, this should be in the form of a reduced fraction.



# **Teaching Fractions**

# **Concrete, Pictorial and Abstract approach**

Concrete and pictorial representations of mathematics are chosen carefully to help build procedural and conceptual knowledge together.

**Concrete** - the "doing" stage, using concrete objects to model problems.

**Pictorial** - the "seeing" stage, using representations of the objects to model problems. Building or drawing a model makes it easier for children to grasp concepts they traditionally find more difficult as it helps them visualise the problem and make it more accessible.

**Abstract** - the "symbolic" stage, where children are able to use abstract symbols to model problems

Although CPA have been presented as three distinct stages, a skilled teacher will go back and forth between each representation to reinforce concepts.

'Used well, manipulatives can enable pupils to inquire themselves- becoming independent learners and thinkers. They can also provide a common language with which to communicate cognitive models for abstract ideas.'

Drury, H. (2015)

Throughout all fraction work the following vocabulary should be referred to and used by teachers and children.

# <u>Part</u> Whole

# <u>Numerator</u> Denominator

**Equal parts of a whole** must be reinforced. The whole could be a shape, a length a set of objects, a number etc. Children must experience fractions in many different contexts.

# **Reception**

# I can solve problems involving distributing quantities equally.

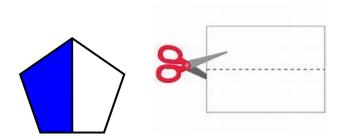
**Concrete:** Throughout Reception children should experience what a half looks like in a wide range of contexts and what a half doesn't look like. The half of something needs to be explored in many concrete situations.

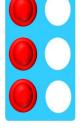


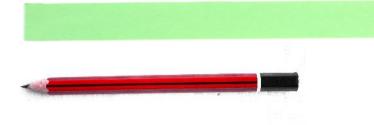
# <u>Year 1</u>

# Recognise, find and name a half as one of two equal parts and a quarter as one of four equal parts of an object, shape or quantity

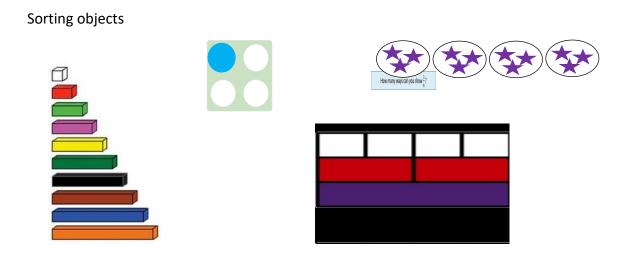
**Concrete:** Children should build on the concrete examples used in Reception to further their understanding of a half. Children should continue to experience what a half looks like in a wide range of contexts and also what a half doesn't look like. Children must have a secure understanding that a half is **two equal parts** of a whole and a quarter **is four equal parts** of a whole through a variety of concrete examples.





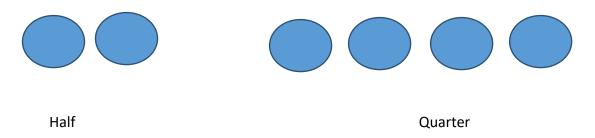


The pencil is half the length of the piece of paper



# Pictorial:

Children use sorting circles to find half and a quarter of quantities



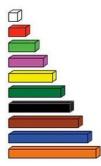
# Children then progress onto a bar model

## <u>Year 2</u>

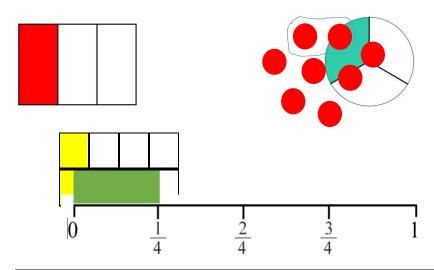
Recognise, name, write and find fractions 1/3;  $\frac{1}{3}$ ;  $\frac{1}{2}$  and  $\frac{3}{4}$  of a length, shape, set of objects or quantity.

*Concrete:* Children continue to build on concrete models used in Year 1 to further their understanding of fractions. Children must recognise and have a secure understanding that a third is **three equal parts** of a whole and three quarters is the value of **3 equal parts of the 4 equal parts that makes up the whole**.





Pictorial: Children should draw diagrams of fractions.



# Children use sorting circles to find a third and three quarters of a quantity



Third

**Three Quarters** 

Children then progress onto a bar model

l .	l	

?

# Recognise the equivalence of 2/4 and 1/2

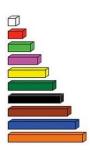
# Concrete:

1

Practical activities, using the same size strips of paper can support with the concept of 'equivalence'. Strips rather than circles are best to use when comparing because they can be placed above/below each other **but children should not only see fractions in a rectangle.** 

	1				3	
						1
4						
1	1/-				No.	「主
31		2	1	W.I.		11
411	1	E.	the de	10	E	and the

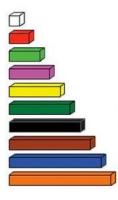
Pictorial: Children draw equivalent fractions

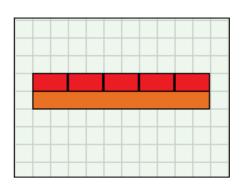


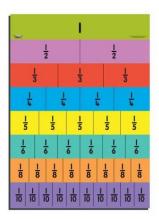
## <u>Year 3</u>

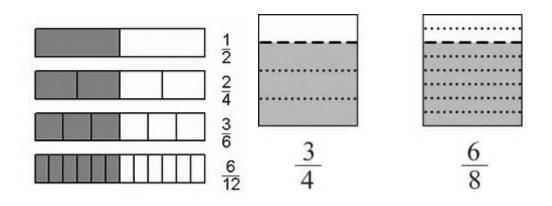
Recognise and show, using diagrams, equivalent fractions for halves, quarters, thirds, fifths, sixths and eighths

**Concrete:** Building on Year 2 practical examples using the same size strips of paper can support with the concept of 'equivalence'. Strips rather than circles are best to use when comparing because they can be placed above/below each other *but children should not only see fractions in a rectangle.* 



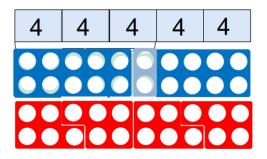






### Recognise fractions as a division of a quantity

**Concrete:** Building on Year 2 and 3, children should use cubes and Cuisenaire rods to provide a concrete example of the concept. Extend this in Year 4 to using numicon e.g 1/5 of 20



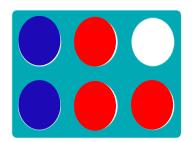
*Pictorial:* Building on year 2, children should use bar model as a pictorial representation. E.g 1/6 of 24

4	4	4	4	4	4

## Add and subtract fractions with a common denominator

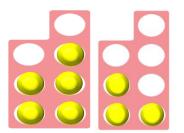
#### Concrete:

Use numicon as a concrete representation e.g 2/6 + 3/6 =



5/7 - 2/7 =

Use numicon as a concrete representation e.g 5/7 - 2/7 =

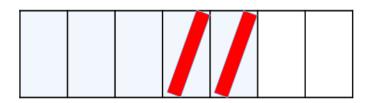


Pictorial:

Use bar model as a pictorial representation e.g. 2/6 + 3/6 =

Recognise fractions as a division of a quantity

5/7 - 2/7 =



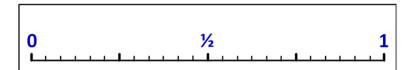
<u>Year 4</u>

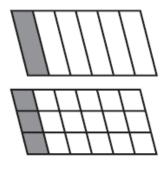
Recognise and show, using diagrams, families of common equivalent fractions

*Concrete:* If required, use the concrete representations from Year 3.

## **Pictorial:**

Continue to build on the pictorial representations in Year 3 and extend to include



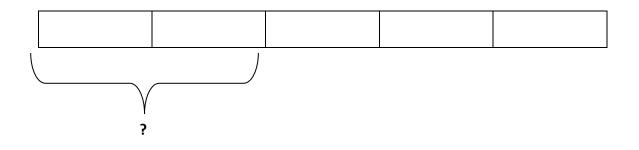


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Solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including non-unit fractions where the answer is a whole number.

*Concrete:* If required use concrete representations from Year 3.

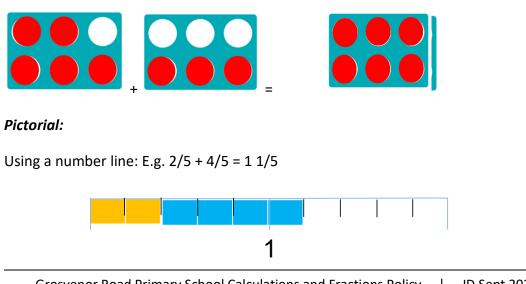
*Pictorial:* Building on the bar model used in Year 3. E.g. 2/5 of 45



Add and subtract fractions with the same denominator, including improper fractions

Concrete:

If required, use the concrete representations from Years 3 for adding and subtracting fractions less than zero. 5/6 + 3/6 =



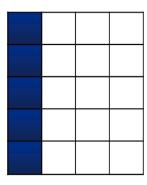
<u>Year 5</u>

Compare and order fractions with denominators that are all multiples

**Concrete:** If required, use the concrete examples in Years 3 and 4 to develop children's understanding of equivalent fractions.

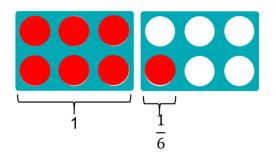
**Pictorial:** 

Use arrays. E.g Which is bigger ¼ or 2/5?



Recognise mixed numbers and improper fractions and convert from one to the other

**Concrete:** Use numicon. For example, 1 1/6 = 7/6



*Pictorial:* Use a bar model to convert between fractions.

Add and subtract fractions with denominators that are all multiples

**Concrete:** If required, use the concrete examples in Years 3 and 4 to develop children's understanding of adding and subtracting fractions with same denominators.

**Pictorial:** If required, use the pictorial examples in Years 3 and 4 to develop children's understanding of adding and subtracting fractions with same denominators.

Array. For example, 1/3 and 2/4 = 10/12 = 5/6

_ 1					

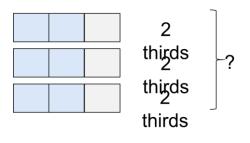
# Multiply proper and mixed number fractions by whole numbers

*Concrete:* Use numicon, for example 2/3 x 3 =





Pictorial: Use bar method, for example 2/3 x 3 =



# <u>Year 6</u>

# Compare and order fractions including fractions > 1

# Concrete and Pictorial:

If required, use the concrete and pictorial models to compare fractions up to 1. Use abstract approach for fractions greater than 1.

# Add and subtract fractions with different denominators and mixed numbers

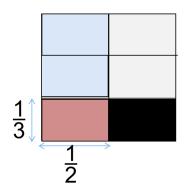
# Concrete and Pictorial:

If required, use the concrete and pictorial models to add fractions with denominators that are multiples from Year 5, then use abstract approach for different denominators and mixed numbers.

# Multiply simple pairs of proper fractions, writing the answer in its simplest form

# **Pictorial:**

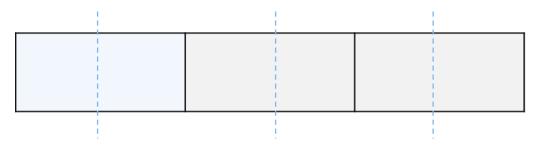
Arrays, for example:  $1/3 \times \frac{1}{2} =$ 



Divide proper fractions by whole numbers ( $\frac{1}{3} \div 2 = 1/16$ )

# Concrete:

Use fraction strips to create a concrete representation, for example  $1/3 \div 2 =$ 



## Pictorial:

Children use a diagram to represent the above.

# Maths Vocabulary Key Stage Two (also in KS2 Pupil Planner)

Year 3	Year 4
Tear 5	(all Y3 vocabulary plus the following-)
Number Disco Value	
Number – Place Value	Number – Place Value Roman numerals, round, nearest, approximately,
2-digit, base 10, pattern, sequence, hundred, partition, recombine, thousand, 3-digit, ascending, descending	negative, minus, tenths, hundredths
Number – Addition & Subtraction	Number – Addition & Subtraction
Bar model, operation, inverse operation, column, exchange, bridge, method, column addition and subtraction, regroup, efficient, estimate.	Formal methods
Number – Multiplication & Division	Number – Multiplication & Division
Times-table, facts, multiples, repeated addition, lots of, multiply, multiplied by, times, commutative, array, go into, divide, divide between, division, dividing, grouping, sharing, remainder, divisor, dividend, quotient.	Product, associative law, commutativity, factor, factor pair.
Number - Fractions	Number - Fractions
unit fraction, numerator, denominator, equivalence, equivalent, non-unit fraction, decimal, decimal point.	Proper fraction, improper fraction, mixed number
Measurement	Measurement
Change, total, distance; metres, g/kg, ml/l, temperature, thermometer, degrees Celsius, increase, decrease, warmer, colder, quarter past/to, start, duration, end, interval, cm, mm, perimeter, leap year, minutes past/to; a.m., p.m., analogue, digital, twelve-hour /twenty-four- hour clock.	km, rectilinear, area, cm squared, square cm, warmest, coldest.
Geometry – Shape, Position &	Geometry – Shape, Position &
Direction	Direction
Pentagon, hexagon, octagon, quadrilateral, prism, vertices, vertex; rotate, symmetry, symmetrical, line of symmetry; horizontal, vertical, fold, pattern, repeating pattern. direction, forwards, backwards, right angle, rotation, clockwise, anticlockwise, parallel, perpendicular, surface, acute angle, obtuse angle, North, South, East, West.	Isosceles, scalene, equilateral, rhombus, parallelogram, trapezium; regular polygon, mirror line, reflect, coordinates, translation, first quadrant, x-axis, y-axis.
Data Handling	Data Handling
Count, tally, tally chart, table, data, represent, sort, pictogram, symbol, block diagram, axis, label, title, scale, most popular, most common, least popular, least common, Venn diagram, Carrol diagram, bar chart, frequency table.	Continuous data, discrete data, line graph, x-axis, y-axis.

Year 5	Year 6
(all Y3, Y4 vocabulary plus the following-)	(all Y3, Y4, Y5 vocabulary plus the following-)
Number – Place Value	Number – Place Value
Numbers to a million; Roman numerals to one thousand; powers of 10.	Algebra: function, input, output, algebra, algebraic, rule, expression, substitute, formula, formulae, equation, value, possible values, enumerate.
Number – Addition & Subtraction	Number – Addition & Subtraction
Place holder.	
Number – Multiplication & Division	Number – Multiplication & Division
Common factor, prime number, composite number, prime factor, square number, cubed number, round up/down.	Order of operations, BIDMAS, common multiple, lowest common multiple.
Number - Fractions	Number - Fractions
Common denominator, thousandth, simplify, simplified, convert, per cent, percentage, per hundred.	Cancel, highest common factor, common denominator, ratio, proportion, enlargement, scale factor.
Measurement	Measurement
Imperial units, metric units, inches, lbs, pints, timetable, compound shape, volume, capacity, cm cubed/cubic cm.	Tonnes, ounces, stone, miles, vertically opposite (angles), internal angles, circumference, radius, diameter, centre.
Geometry – Shape, Position &	Geometry – Shape, Position &
Direction	Direction
Degrees, protractor, reflex angle, irregular polygon, dimensions, net, reflection, reflect.	Four quadrants.
Data Handling	Data Handling
	mean, pie chart, minimum, maximum, range

Addition	Subtraction	Multiplication	Division
add	subtract	multiply	divide
plus	minus	times	divided by
and	take	lots of	division
more	take away	groups of	share
altogether	difference	product	shared by
total	less		split
sum of	decrease		half
increase	deficit		
addition	reduce		